

```
In[1]:= Needs ["SpinDynamica`"]
```

```
SpinDynamica version 3.0.1 loaded
```

... **ModifyBuiltin**: The following built-in routines have been modified in SpinDynamica:
{Chop, Dot, Duration, Exp, Expand, ExpandAll, NumericQ, Plus, Power, Simplify, Times, WignerD}.
Evaluate ??symbol to generate the additional definitions for symbol.

1 spin-1/2

```
In[2]:= SetSpinSystem[1]
```

... **SetSpinSystem**: the spin system has been set to $\left\{\left\{1, \frac{1}{2}\right\}\right\}$

... **SetBasis**: the state basis has been set to ZeemanBasis $\left[\left\{\left\{1, \frac{1}{2}\right\}\right\}, \text{BasisLabels} \rightarrow \text{Automatic}\right]$.

```
In[3]:= OperatorBasis []
```

... **SetOperatorBasis**: the operator basis has been set to ShiftAndZOperatorBasis $\left[\left\{\left\{1, \frac{1}{2}\right\}\right\}, \text{Sorted} \rightarrow \text{CoherenceOrder}\right]$.

```
Out[3]= ShiftAndZOperatorBasis [ { { 1, 1/2 } }, Sorted -> CoherenceOrder ]
```

```
In[4]:= BasisOperators []
```

```
Out[4]= { I1, sqrt(2) I1z, I1/sqrt(2), I1 }
```

```
In[5]:= OperatorVectorRepresentation [
  opI ["x"]
] // MatrixForm
```

```
Out[5]/MatrixForm=
```

$$\begin{pmatrix} 1 \\ 2 \\ 0 \\ 0 \\ \frac{1}{2} \end{pmatrix}$$

```
In[6]:= SuperoperatorMatrixRepresentation [
  UnitySuperoperator []
] // MatrixForm
```

```
Out[6]/MatrixForm=
```

$$\begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

```
In[7]:= SuperoperatorMatrixRepresentation [
  NullSuperoperator []
] // MatrixForm
```

```
Out[7]/MatrixForm=
```

$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

```
In[8]:= SuperoperatorMatrixRepresentation[
  CommutationSuperoperator[opI["z"]]
] // MatrixForm
```

```
Out[8]//MatrixForm=

$$\begin{pmatrix} -1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

```

```
In[9]:= SuperoperatorMatrixRepresentation[
  CommutationSuperoperator[opI["x"]]
] // MatrixForm
```

```
Out[9]//MatrixForm=

$$\begin{pmatrix} 0 & \frac{1}{\sqrt{2}} & 0 & 0 \\ \frac{1}{\sqrt{2}} & 0 & 0 & -\frac{1}{\sqrt{2}} \\ 0 & 0 & 0 & 0 \\ 0 & -\frac{1}{\sqrt{2}} & 0 & 0 \end{pmatrix}$$

```

```
In[10]:= SuperoperatorMatrixRepresentation[
  DoubleCommutationSuperoperator[opI["x"], opI["x"]]
] // MatrixForm
```

```
Out[10]//MatrixForm=

$$\begin{pmatrix} \frac{1}{2} & 0 & 0 & -\frac{1}{2} \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ -\frac{1}{2} & 0 & 0 & \frac{1}{2} \end{pmatrix}$$

```

```
In[11]:= SuperoperatorMatrixRepresentation[
  RotationSuperoperator[{ $\pi/2$ , "x"}]
] // MatrixForm
```

```
Out[11]//MatrixForm=

$$\begin{pmatrix} \frac{1}{2} & -\frac{i}{\sqrt{2}} & 0 & \frac{1}{2} \\ -\frac{i}{\sqrt{2}} & 0 & 0 & \frac{i}{\sqrt{2}} \\ 0 & 0 & 1 & 0 \\ \frac{1}{2} & \frac{i}{\sqrt{2}} & 0 & \frac{1}{2} \end{pmatrix}$$

```

2 spins-1/2

```
In[12]:= SetSpinSystem[2]
```

... **SetSpinSystem**: the spin system has been set to $\{\{1, \frac{1}{2}\}, \{2, \frac{1}{2}\}\}$

... **SetBasis**: the state basis has been set to ZeemanBasis $\{\{\{1, \frac{1}{2}\}, \{2, \frac{1}{2}\}\}, \text{BasisLabels} \rightarrow \text{Automatic}\}$.


```
In[23]:= SuperoperatorMatrixRepresentation[
  Exp[-I (π/2) CommutationSuperoperator[2 opI[1, "z"].opI[2, "z"]]]
] // MatrixForm
```

Out[23]//MatrixForm=

$$\begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

perform product-operator style calculations

```
In[24]:= ExpressOperator[
  RotationSuperoperator[1, {β, "x"}][2 opI[1, "z"].opI[2, "z"]]
] // Simplify
```

Out[24]= $2 \cos[\beta] (I_{1z} \cdot I_{2z}) - 2 (I_{1y} \cdot I_{2z}) \sin[\beta]$

```
In[25]:= ExpressOperator[
  Exp[-I (π/2) CommutationSuperoperator[2 opI[1, "z"].opI[2, "z"]]] [opI[1, "x"]]
] // Simplify
```

Out[25]= $2 (I_{1y} \cdot I_{2z})$