

# REDOR

tested 190817 using *SpinDynamica* 3.0.1 under *Mathematica* 11.0

## init

```
Needs["SpinDynamica`"]
```

```
SpinDynamica version 3.0.1 loaded
```

**ModifyBuiltIn:** The following built-in routines have been modified in SpinDynamica:

{Chop, Dot, Duration, Exp, Expand, ExpandAll, NumericQ, Plus, Power, Simplify, Times, WignerD}.

Evaluate ??symbol to generate the additional definitions for symbol.

## code

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## spin system & Hamiltonians

### define heteronuclear 2-spin-1/2 system

```
SetSpinSystem[{ {"I", 1/2}, {"S", 1/2}}]
```

**SetSpinSystem:** the spin system has been set to  $\{\{I, \frac{1}{2}\}, \{S, \frac{1}{2}\}\}$

**SetBasis:** the state basis has been set to ZeemanBasis[ $\{\{I, \frac{1}{2}\}, \{S, \frac{1}{2}\}\}$ , BasisLabels → Automatic].

### heteronuclear 2-spin-1/2 Hamiltonian in a rotating solid

```
wIS[t_, ωMR_] := {0, 0, bIS, 0, 0}.WignerD[2, {{0}}][{ΩPMIS, ωMR, {αRLθ - ωr t, βRL, 0}}]

HIS[ωMR_] := PeriodicFunction[t,
  Evaluate[(2 π / ωr)],
  Evaluate@Chop@N[wIS[t, ωMR] 2 opI["I", "z"].opI["S", "z"]]]
]
```

## example

```
 $\Omega_{PMIS} = \{0, 0, 0\};$ 
 $\Omega_{MR} = \{0, \pi/2, 0\};$ 
 $\alpha_{RL0} = 0;$ 
 $HIS[\Omega_{MR}]$ 
```

**WignerD:** The built-in function WignerD has been given extra functionality in SpinDynamica. Execute ?WignerD for more information.

For ?WignerD click [here](#)

```
PeriodicFunction[t,  $\frac{2\pi}{\omega r}$ ,
2. bIS  $(I_z \cdot S_z) (0.5 (0.5 - 1.5 \text{Cos}[\beta RL]^2) + 0.612372 (0.306186 \times 2.71828^{(0.-2.\imath)} t \omega r -$ 
 $0.306186 \times 2.71828^{(0.-2.\imath)} t \omega r \text{Cos}[0.5 \beta RL]^4 + 1.83712 \times 2.71828^{(0.-2.\imath)} t \omega r$ 
 $\text{Cos}[0.5 \beta RL]^2 \text{Sin}[0.5 \beta RL]^2 - 0.306186 \times 2.71828^{(0.-2.\imath)} t \omega r \text{Sin}[0.5 \beta RL]^4) +$ 
 $0.612372 (0.306186 \times 2.71828^{(0.+2.\imath)} t \omega r - 0.306186 \times 2.71828^{(0.+2.\imath)} t \omega r \text{Cos}[0.5 \beta RL]^4 +$ 
 $1.83712 \times 2.71828^{(0.+2.\imath)} t \omega r \text{Cos}[0.5 \beta RL]^2 \text{Sin}[0.5 \beta RL]^2 -$ 
 $0.306186 \times 2.71828^{(0.+2.\imath)} t \omega r \text{Sin}[0.5 \beta RL]^4))]$ 
```

## default parameters

default parameters (5 kHz spinning frequency, 200Hz dipolar coupling)

```
 $\omega r = 2\pi 5 \times 10^3;$ 
 $\beta RL = \text{ArcTan}[\text{Sqrt}[2]];$ 
 $bIS = 2\pi 200;$ 
 $\Omega_{PMIS} = \{0, 0, 0\};$ 
 $\Omega_{MR} = \{0, \pi/4, 0\};$ 
 $\alpha_{RL0} = 0;$ 
 $\tau r = 2\pi / \omega r$ 
 $\frac{1}{5000}$ 
```

define REDOR sequence

```
REDORsequence[n_] :=
{
  Repeat[
    {
      {None, τr/2},
      RotationSuperoperator["S", {π, 0}],
      {None, τr/2},
      RotationSuperoperator["S", {π, 0}]
    }, n
  ],
  RotationSuperoperator["I", {π, 0}],
  Repeat[
    {RotationSuperoperator["S", {π, 0}],
     {None, τr/2},
     RotationSuperoperator["I", {π, 0}],
     {None, τr/2}
    }, n
  ],
  RotationSuperoperator["I", {π/2, 0}]
};
```

## calculations

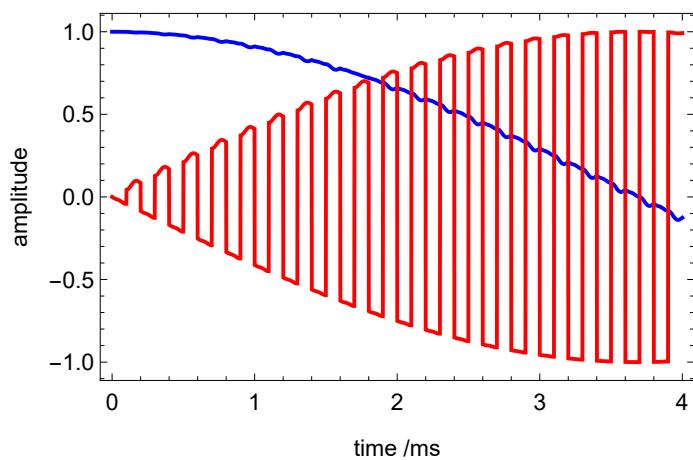
calculate trajectories of in-phase and antiphase magnetization, during the REDOR sequence, for a single molecular orientation

$$\Omega_{MR} = \{0, \pi/3, \pi/3\};$$

**trajectories of I-spin x-magnetization (blue) and antiphase 2IySz terms (red) during the sequence**

```
{Ixtraj, IySztraj} = Trajectory[
  opI["I", "x"] -> {opI["I", "x"], 2 opI["I", "y"].opI["S", "z"]},
  REDORsequence[10],
  BackgroundGenerator → HIS[ΩMR]
]
{TrajectoryFunction[ {{0, 4. × 10⁻³}} , <>], TrajectoryFunction[ {{0, 4. × 10⁻³}} , <>]}
```

```
Plot[{Re@Ixtraj[tms  $\times 10^{-3}$ ] , Re@IySztraj[tms  $\times 10^{-3}$ ] },
 {tms, 0, 10 $^3 \times$  EventDuration[REDORsequence[10]]},
 Frame  $\rightarrow$  True, PlotStyle  $\rightarrow$  {{Thick, Blue}, {Thick, Red}},
 LabelStyle  $\rightarrow$  Directive[Medium, FontFamily  $\rightarrow$  "Helvetica"],
 FrameLabel  $\rightarrow$  {"time /ms", "amplitude"}]
```



note how the antiphase terms (red) build up while the in-phase terms (blue) decay

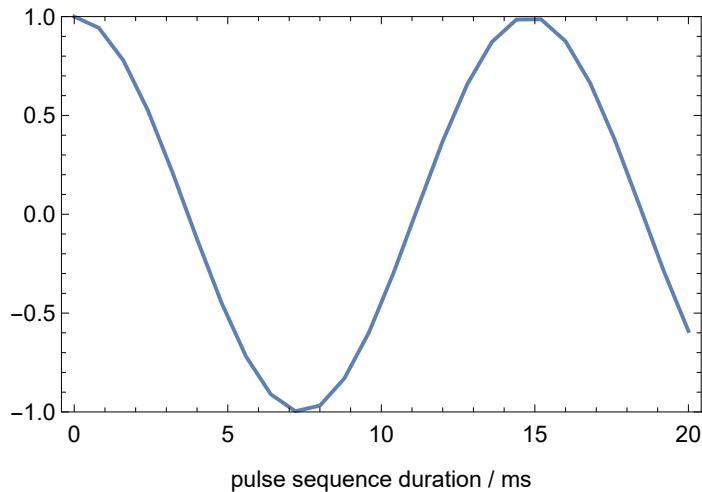
## single orientation

```
ListPlot[
 TransformationAmplitudeTable[
  opI["I", "x"] -> opI["I", "x"],
  REDORsequence[n],
  {n, 0, 50, 2},
  BackgroundGenerator -> HIS[ΩMR],
  TableCoordinates -> EventDuration[REDORsequence[n]] × 10^3
 ],
 Joined -> True, Frame -> True, PlotStyle -> Thick, PlotRange -> {-1, 1},
 FrameLabel -> {"pulse sequence duration / ms", None},
 LabelStyle -> Directive[Medium, FontFamily -> "Helvetica"]
]
```

Get: Cannot open CloudObjectLoader`.

SetOperatorBasis: the operator basis has been set to

ShiftAndZOperatorBasis[{ $\{I, \frac{1}{2}\}$ ,  $\{S, \frac{1}{2}\}$ }, Sorted -> CoherenceOrder].



calculate powder average trajectory of in-phase magnetization (REDOR curve)

## powder average

```

ΩMR = .;
table =
  TransformationAmplitudeTable[
    opI["I", "x"] -> opI["I", "x"],
    REDORsequence[n],
    {n, 0, 50, 2},
    BackgroundGenerator -> HIS[ΩMR],
    TableCoordinates -> EventDuration[REDORsequence[n]] × 10^3,
    EnsembleAverage -> {ΩMR, OrientationsAndWeights["ZCW50"]}
  ];
Predefined orientational sampling schemes:
{Leboct10, Leboct16, Leboct19, Leboct22, Leboct31, Leboct37, Leboct46,
 Leboct85, POLYTOPE12, POLYTOPE60, Random $\alpha\beta$ , Random $\alpha\beta\gamma$ , Random $\beta$ , REPULSION100,
 REPULSION150, REPULSION168, REPULSION232, REPULSION376, REPULSION700,
 Step $\alpha\beta$ , Step $\beta$ , ZCW1154, ZCW144, ZCW200, ZCW300, ZCW50, ZCW538, ZCW6044}
Execute OrientationalSamplingScheme[scheme] for the usage message of a sampling scheme.
```

```

ListPlot[
 Re@table,
 Joined -> True, Frame -> True, PlotStyle -> Thick, PlotRange -> All, Axes -> True,
 FrameLabel -> {"pulse sequence duration / ms", None},
 LabelStyle -> Directive[Medium, FontFamily -> "Helvetica"]
]

```

