

In[1]:= Needs ["SpinDynamica`"]

SpinDynamica version 3.0.1 loaded

... **ModifyBuiltin**: The following built-in routines have been modified in SpinDynamica:  
{Chop, Dot, Duration, Exp, Expand, ExpandAll, NumericQ, Plus, Power, Simplify, Times, WignerD}.  
Evaluate ??symbol to generate the additional definitions for symbol.

In[2]:= SetSpinSystem[2]

... **SetSpinSystem**: the spin system has been set to  $\left\{\left\{1, \frac{1}{2}\right\}, \left\{2, \frac{1}{2}\right\}\right\}$

... **SetBasis**: the state basis has been set to ZeemanBasis $\left[\left\{\left\{1, \frac{1}{2}\right\}, \left\{2, \frac{1}{2}\right\}\right\}, \text{BasisLabels} \rightarrow \text{Automatic}\right]$ .

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## bases

### ZeemanBasis

In[3]:= Basis[]

Out[3]= ZeemanBasis $\left[\left\{\left\{1, \frac{1}{2}\right\}, \left\{2, \frac{1}{2}\right\}\right\}, \text{BasisLabels} \rightarrow \text{Automatic}\right]$

In[4]:= BasisKets[]

Out[4]=  $\{|\alpha\alpha\rangle, |\beta\alpha\rangle, |\alpha\beta\rangle, |\beta\beta\rangle\}$

In[5]:= BasisBras[]

Out[5]=  $\{\langle\alpha\alpha|, \langle\beta\alpha|, \langle\alpha\beta|, \langle\beta\beta|\}$

In[6]:= MatrixRepresentation[opI["y"]] // MatrixForm

Out[6]/MatrixForm=

$$\begin{pmatrix} 0 & -\frac{i}{2} & -\frac{i}{2} & 0 \\ \frac{i}{2} & 0 & 0 & -\frac{i}{2} \\ \frac{i}{2} & 0 & 0 & -\frac{i}{2} \\ 0 & \frac{i}{2} & \frac{i}{2} & 0 \end{pmatrix}$$

### SingletTripletBasis

In[7]:= SetBasis[SingletTripletBasis[]]

... **SetBasis**: the state basis has been set to SingletTripletBasis $\left[\left\{\left\{1, \frac{1}{2}\right\}, \left\{2, \frac{1}{2}\right\}\right\}, \text{BasisLabels} \rightarrow \text{Automatic}\right]$ .

In[8]:= BasisKets[]

Out[8]=  $\left\{\frac{-|\beta\alpha\rangle + |\alpha\beta\rangle}{\sqrt{2}}, |\alpha\alpha\rangle, \frac{|\beta\alpha\rangle + |\alpha\beta\rangle}{\sqrt{2}}, |\beta\beta\rangle\right\}$

In[9]:= BasisBras[]

Out[9]=  $\left\{\frac{-\langle\beta\alpha| + \langle\alpha\beta|}{\sqrt{2}}, \langle\alpha\alpha|, \frac{\langle\beta\alpha| + \langle\alpha\beta|}{\sqrt{2}}, \langle\beta\beta|\right\}$

```
In[10]:= MatrixRepresentation[opI["y"]] // MatrixForm
```

```
Out[10]//MatrixForm=
```

$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & -\frac{i}{\sqrt{2}} & 0 \\ 0 & \frac{i}{\sqrt{2}} & 0 & -\frac{i}{\sqrt{2}} \\ 0 & 0 & \frac{i}{\sqrt{2}} & 0 \end{pmatrix}$$

## Eigenbasis

```
In[11]:= SetBasis[Eigenbasis[opI["x"]]]
```

... **CheckBasis**: State basis is orthonormal.

... **SetBasis**: the state basis has been set to Eigenbasis $\left[|1_x + 1_{2x}\rangle, \left\{\left\{1, \frac{1}{2}\right\}, \left\{2, \frac{1}{2}\right\}\right\}, \text{BasisLabels} \rightarrow \text{Automatic}\right]$ .

```
In[12]:= BasisKets[]
```

$$\text{Out[12]} = \left\{ \frac{|\beta\beta\rangle}{2} - \frac{|\beta\alpha\rangle}{2} - \frac{|\alpha\beta\rangle}{2} + \frac{|\alpha\alpha\rangle}{2}, \frac{|\beta\beta\rangle}{2} + \frac{|\beta\alpha\rangle}{2} + \frac{|\alpha\beta\rangle}{2} + \frac{|\alpha\alpha\rangle}{2}, \frac{|\beta\beta\rangle}{\sqrt{2}} - \frac{|\alpha\alpha\rangle}{\sqrt{2}}, -\frac{|\beta\alpha\rangle}{\sqrt{2}} + \frac{|\alpha\beta\rangle}{\sqrt{2}} \right\}$$

```
In[13]:= BasisBras[]
```

$$\text{Out[13]} = \left\{ \frac{\langle\beta\beta|}{2} - \frac{\langle\beta\alpha|}{2} - \frac{\langle\alpha\beta|}{2} + \frac{\langle\alpha\alpha|}{2}, \frac{\langle\beta\beta|}{2} + \frac{\langle\beta\alpha|}{2} + \frac{\langle\alpha\beta|}{2} + \frac{\langle\alpha\alpha|}{2}, \frac{\langle\beta\beta|}{\sqrt{2}} - \frac{\langle\alpha\alpha|}{\sqrt{2}}, -\frac{\langle\beta\alpha|}{\sqrt{2}} + \frac{\langle\alpha\beta|}{\sqrt{2}} \right\}$$

```
In[14]:= MatrixRepresentation[opI["y"]] // MatrixForm
```

```
Out[14]//MatrixForm=
```

$$\begin{pmatrix} 0 & 0 & \frac{i}{\sqrt{2}} & 0 \\ 0 & 0 & -\frac{i}{\sqrt{2}} & 0 \\ -\frac{i}{\sqrt{2}} & \frac{i}{\sqrt{2}} & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

```
In[15]:= MatrixRepresentation[opI["x"]] // MatrixForm
```

```
Out[15]//MatrixForm=
```

$$\begin{pmatrix} -1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

## BasisLabels

```
In[16]:= ? BasisLabels
```

*BasisLabels* is an option for the Hilbert space bases. If *BasisLabels*  $\rightarrow$  *Automatic* (default), the Kets and Bras may be referred to using integers running from 1 to the basis dimension. The option *BasisLabels*  $\rightarrow$   $\{a,b,c,\dots\}$  allows the integers or strings  $\{a,b,c,\dots\}$  to be used to refer to the Kets and Bras. The operation *BasisLabels*[*basis*] may also be used to obtain the set of state labels defined for a particular basis.

```
In[17]:= SetBasis[]
```

... **SetBasis**: the state basis has been set to ZeemanBasis $\left[\left\{\left\{1, \frac{1}{2}\right\}, \left\{2, \frac{1}{2}\right\}\right\}, \text{BasisLabels} \rightarrow \text{Automatic}\right]$ .

In[18]:= **BasisLabels** []

Out[18]= {1, 2, 3, 4}

In[19]:= **Ket** [1]

Out[19]=  $|\alpha\rangle$

In[20]:= **Bra** [3]

Out[20]=  $\langle\alpha\beta|$

In[21]:= **SetBasis** [ZeemanBasis [BasisLabels  $\rightarrow$  {0, 1, 2, 3}]]

 **SetBasis**: the state basis has been set to ZeemanBasis[{{1,  $\frac{1}{2}$ }, {2,  $\frac{1}{2}$ }}, BasisLabels  $\rightarrow$  {0, 1, 2, 3}].

In[22]:= **Ket** [0]

Out[22]=  $|\alpha\rangle$

In[23]:= **Bra** [3]

Out[23]=  $\langle\beta\beta|$