Technological resources that come with mathematics textbooks: potentials and constraints

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Introduction

• Traditionally in educational systems:
  • there is a strong tradition of using textbooks;
  • occasionally textbooks are accompanied by technological tools (CD-ROMs, web pages or learning platforms);
  • the curriculum modelled by teachers is based mainly on the use of the textbook adopted in paper format;
  • often teachers use some technological tools associated with textbooks, especially those that do not involve student’s manipulation (eg. ppoints);
Introduction

- This presentation is about the use of technological tools in the context of the classroom.

- It is based on the curriculum presented to teachers, through textbooks and electronic materials and the aim is to explain how these materials become learning tools.

- This study is based in one of the technological mediators available by one of the Portuguese publishing houses, *Escola Virtual*, that is highly structured, following the sequence of learning presented in the textbook on paper.
Theoretical framework

- *Activity Theory* (Vygotsky, Leont'ev), assuming its system of collective activity (object oriented and mediated by artifacts).  
  (Engeström, 2001)

- The concept of *instrumental genesis* that involves two processes: *instrumentalization* and *instrumentation*. These processes enable the development and evolution of the instruments.  
  (Rabardel, 1995)

- The notion of *documentational genesis*. It is a construct that expands the concept of artifact by defining the notion of document as building utilization schemes in teachers action mediated by didactical resources.  
  (Gueudet and Trouche, 2012)
Methodology

• This study follows a methodology of qualitative nature and is based on two case studies.

• Involve two groups of secondary school students that use mainly textbooks, and this was the first time that they used the electronic resource as a learning tool.

• Each case study involves several work sessions with the tool. One case is centered on the theme of functions and the other in geometry.
Methodology

- Students are organized in groups of two.
- Working sessions were recorded by special software that records sound and all actions carried out on the computer screen.
- Contents have not been addressed previously by the teacher.
- The process of instrumental genesis started simultaneously with the learning process.
Learning environment *(Escola Virtual)*

- Two topics:
  - quadratic functions;
  - Cartesian geometry.

- These case studies are based on the use of a CD ROM.
Implementation of the learning environment

• Initially students followed the structure of the lesson presented in the tool, with some differences:
  • students who studied the quadratic function had a guiding worksheet to explore the tool;
  • students who have studied geometry followed the topics presented in the tool and then they used a worksheet with exercises provided by the teacher.

• Students have appropriated quickly the use of the tool and the instrumentalization process was relatively short.

• The didactic proposal presented in the tool sometimes did not promote the learning of concepts. In both cases, the teacher provided worksheets.
Potentials of the tool

- The instrumentation process was short due to the high degree of the structuring of concepts presentation.

Alberto - The 1st video explains well the definition of concavity of a graph of a function at a given interval. You understand Elisabete?

Elisabete - Yes. The graph has a concavity facing upwards if in that range is above all lines tangent to the curve. Is this correct what I said?

Alberto - Okay. Now come to the 2nd and 3rd videos. The signal of $a$, the coefficient of the term of degree 2, the quadratic function, varies the direction of the concavity of the parabola. Correct?

Elisabete - Yeah, I get it. And the greater the absolute value of $a$ the parabola more approaches the ordinate axis.
Potentials of the tool

- Learning concepts is highly potentiated by the possibility of manipulate different representations of the concept (e.g., the manipulation of selectors).

Elisabete - The 1st video consolidates what we learned earlier: the parameter $a$ will cause the parabola stretch or shrink horizontally.

Alberto - Explain yourself better!

Elisabete - Notice that the longer the absolute value of $a$ more parabola closes around the y-axis.

Alberto - Okay, let’s now see the $h$ in $(x-h)^2$?

Elisabete - The parabola moves horizontally to the right and to the left, when we change $h$.

Alberto - And it is the x-coordinate of the vertex of the parabola.

Elisabete - I get it! And the $k$ does the parabola go up or down. And is the ordinate of the vertex.
Potentials of the tool

- Motivation increased with the performance of self-corrective tasks providing competition among students.

- Self-corrective tasks improve performance of algebraic procedures even when these are routine.

(Each of the students went to a computer and individually used the CD-ROM to solve the task, proposed by the teacher and based on the exercises of the tool).

Elisabete - Of the 36 possible correct answers I missed 4. I did not hit, for example, in the calculation of the zeros and the coordinates of the vertex of the parabola. But I returned to do this exercise (on the sheet of paper) and found where I went wrong.

Alberto - I got it all at first. Good!
Constraints of the tool

- Formal language used in audio and video texts is hard to grasp.

Alberto - Did you understand the resolution of this problem?

Elisabete - I had difficulty in calculating the values that the length of the rectangle can take.

Alberto - Would you repeat the video?

Elisabete - Yes. [after 2nd visualization of the video] What values can $c$ take? Explain to me this step because the video is not very clear on this point.

Alberto - Consider: the width $l=50-c$ can not be negative or zero. $50-c>0 \iff -c>-50 \iff c<50$.

Elisabete - And $c$ is greater than zero, it is a length. And the value of $c$ which corresponds to a maximum area? How do you find this value without having heard the answer given by the video? Did you notice that the parabola drawn on the CD-ROM does not pass the origin? It is wrong because when $c=0$ the area is zero. We found an error in the CD-ROM!

What is the rectangle of largest area that can be constructed with a cord of 1 meter?
Constraints of the tool

- The use of symbolic representations that students sometimes did not dominate because they are too formal;

Teacher: Let’s see. You are not understand?

Vanessa: No, I'm not realizing.

Teacher: You do not understand what?

Vanessa: I do not understand this thing of signals.

[They hear a little more of the audio of negation]. (…)

Teacher: So what is the question?

Vanessa: It’s here “stor”, I can not understand these expressions.
  [Points to the expressions below]
Constraints of the tool

- Solving self-corrective tasks can be performed without an understanding of the mathematical concepts involved. *Students can use a process of trial and error, correcting their wrong answers.*

- The tool is not *open-access* which restricts its use outside the context of the classroom. *These constraints lead teachers to develop specific kinds of documents.*
Final remarks

- Highly structured technological tools (akin to tutorials) can be good learning tools.

- The process of instrumental genesis can be short when the tool is very structured, but can cause understanding difficulties for less gifted students.

- When computational tools are used, documentational genesis can become a powerful artefact to develop schemes that promote student’s learning.

- The documentational genesis can be developed either based on the potentialities either based on the constraints of the tool.
Thank you for your attention